# CS 784: Computational Linguistics Lecture 17: Pragmatics

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#### Announcements

**Assignment 2**: For GPT-2 conditional entropy/probability calculation, since there is no official start-of-sentence token, we cannot directly calculate a well-defined  $P(w_0)$ . Instead, you may just start from the second word.

**Final Exam**: Apr 11, 2025, 4:00pm-6:30pm, MC 2034. It will be open-book, open-notes, and open-internet.

## Pragmatics: Meanings Beyond Semantics

A diplomat who says yes means maybe, a diplomat who says maybe means no, and a diplomat who says no is no diplomat. —Talleyrand

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—Tallevrand

What one communicates may differ from what one literally says. Pragmatics: the study of the underlying communication intentions and goals of speakers.

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00000

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Stop at the car.

I'm running late.

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- Far-side pragmatics focuses on what happens beyond.



Stop at the car.

Near-side: the speaker is talking about where to park the car (among multiple options).

I'm running late.
Far-side: the speaker is implying that the listener (the driver) should hurry up.

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  - Unclear statements usually carry more information.

A and B are talking about a mutual friend, C, who is now working in a bank. A asks B how C is getting on in his job, and B replies: Oh quite well, I think; he likes his colleagues, and he hasn't been to prison yet.

Q(uantity-1)-based implicature: make your contribution as informative as is required.

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R(elation; quantity-2)-based implicature: say no more than is required.

I broke a finger yesterday.

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R(elation; quantity-2)-based implicature: say no more than is required.

I broke a finger yesterday.

• I broke my own finger. There is no reason to say my finger as it can be inferred.

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- They know (and know that I know that they know) that I can see that the supposition that they think that q is required.
- They have done nothing to stop me thinking that q.
- They intended me to think, or at lease willing to allow me to think, that q; and so they have implicated that q.

## Scalar Implicature

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[Source: Scontras et al.; https://www.problang.org/]

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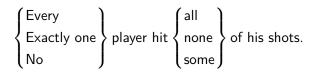
How many apples do you think are red?

**Indirect implicature**: not all means some (i.e., at least one).

#### Embedded Implicature

$$\left\{ \begin{array}{l} \mathsf{Every} \\ \mathsf{Exactly} \ \mathsf{one} \\ \mathsf{No} \end{array} \right\} \mathsf{player} \ \mathsf{hit} \left\{ \begin{array}{l} \mathsf{all} \\ \mathsf{none} \\ \mathsf{some} \end{array} \right\} \mathsf{of} \ \mathsf{his} \ \mathsf{shots}.$$

## Embedded Implicature



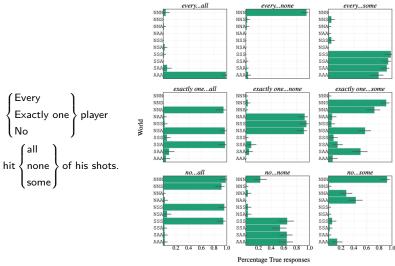


Exactly one player hit some of his shots.



## Embedded Implicature

Humans show clear preferences on world states.



#### Question Under Discussion

I've been waiting for a million years.
I paid one thousand dollars for the coffee.

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Communication intents are relevant to what question under discussion (QUD) a speaker is likely addressing with their utterances.

#### Comparison Class

Look at the **big** tree near the **small** lake.

#### Comparison Class

Look at the big tree near the small lake.

The *small lake* is larger than the *big tree* anyway.

This is because we infer the different comparison classes for them.

#### Overinformativeness and Politeness

(In a coffee shop)

Q: Do you have iced tea?

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People often violate the informativeness rule.

In such a scenario, pragmatic inference happens when choosing the substitution:

- \* No, but we do have muffins.
- \* No, but we do have laptops.



[Source: Frank & Goodman, 2012]



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You and your friend are playing a referential communication game.

The **speaker** knows the correct object and tells the listener.



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- The **speaker** knows the correct object and tells the listener.
- The **listener** picks up **one** object following the speaker's instruction.



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- Both players will be rewarded if the listener picks up the correct object.



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- The speaker knows the correct object and tells the listener.
- The **listener** picks up **one** object following the speaker's instruction.
- Both players will be rewarded if the listener picks up the correct object.
- The speaker can only refer to the intrinsic properties of objects (no "middle" or "left" etc.).



[Source: Frank & Goodman, 2012]

For simplicity, we assume the speakers will only use **color** and/or shape to refer to objects.



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Which object will you pick?



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Suppose you are the **listener** and hear "**square**."

Which object will you pick? Most participants say the **first**.

Suppose you are the **speaker** and want to refer to the third object.

Which word will you use, green or square?



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Suppose you are the listener and hear "square."

Which object will you pick? Most participants say the **first**.

Suppose you are the **speaker** and want to refer to the third object.

Which word will you use, green or square?

A: green as it's less ambiguous.



# The Rational Speech Act (RSA) Framework



[Source: Frank & Goodman, 2012]

Computationally models the process that "square" refers to the first object.



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## The Rational Speech Act (RSA) Framework



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Computationally models the process that "square" refers to the first object.

A Bayesian approach: derive posterior (pragmatics) from the prior (semantics/literal meanings).

We need a set of pre-defined world states (i.e., possible choices) S and possible utterances U:

```
S = \{blue-square, blue-circle, green-square\}
U = \{blue, green, square, circle\}
```

## RSA: Literal Listener $L_0$



[Source: Frank & Goodman, 2012]

 $S = \{ blue-square, blue-circle, green-square \}$  $U = \{$ blue, green, square, circle $\}$ 



#### RSA: Literal Listener $L_0$



[Source: Frank & Goodman, 2012]

$$S = \{ ext{blue-square, blue-circle, green-square} \}$$
  
 $U = \{ ext{blue, green, square, circle} \}$ 

$$P_{L_0}(s \mid u) \propto [\![u]\!](s)P(s)$$

$$\propto \begin{cases} P(s) & \text{if } u \text{ is true for } s \\ 0 & \text{otherwise} \end{cases}$$

$$[blue][blue-square] = 1$$
  $[blue][green-square] = 0$   $[green][green-square] = 1$ 



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Suppose P(s) is uniform over all s, here is  $[\![u]\!](s)P(s)$ :



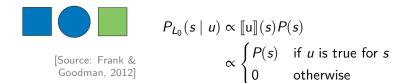
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$U \setminus S$	blue-square	blue-circle	green-square
blue	1/3	1/3	0
green	0	0	1/3
square	1/3	0	1/3
circle	0	1/3	0



 $P_{L_0}$  is a **probability distribution**, so we normalize the table:



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 $S_1$  will choose the utterance u that maximizes the probability of the listener picking the correct object:

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$$P_{S_1}(u \mid s) \propto P_{L_0}(s \mid u)$$

In real-practice,  $S_1$  also considers the cost of utterances.

$$\begin{array}{c} \textit{U}(\textit{u};\textit{s}) = \log \textit{P}_{\textit{S}_{1}}(\textit{u} \mid \textit{s}) - \text{cost}(\textit{u}) & \text{(utility function)} \\ \textit{P}_{\textit{S}_{1}}(\textit{u} \mid \textit{s}) \propto \alpha \exp(\textit{U}(\textit{u};\textit{s})) & (\alpha: \text{ hyperparameter}) \end{array}$$

## RSA: Pragmatic Speaker with an Example



[Source: Frank & Goodman, 2012]

$$U(u; s) = \log P_{S_1}(u \mid s) - \cot(u)$$
  
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Assume 0 cost function and  $\alpha = 1$ ,  $P_{S_1}(u \mid s) \propto P_{L_0}(s \mid u)$ .

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$$P_{L_0}(s \mid u)$$

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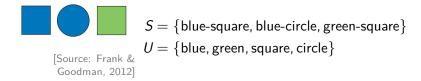
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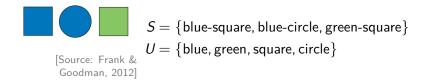
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 $L_1$  will infer the world state s from the utterance u:

$$P_{L_1}(s \mid u) \propto P_{S_1}(u \mid s)P(s)$$

## RSA: Pragmatic Listener with an Example



$$P_{L_1}(s \mid u) \propto P_{S_1}(u \mid s)P(s)$$

[Source: Frank & Goodman, 2012]

Assume uniform prior over world states. Normalize the rows to form a well-defined probability distribution:  $P_{L_1}(s \mid u) \propto P_{S_1}(u \mid s)$ .

$$P_{S_1}(u \mid s)$$

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## Summary: RSA

$$\begin{aligned} P_{L_0}(s \mid u) &\propto \llbracket u \rrbracket(s) P(s) \\ P_{S_1}(u \mid s) &\propto P_{L_0}(s \mid u) \\ U(u; s) &= \log P_{S_1}(u \mid s) - \operatorname{cost}(u) \\ P_{S_1}(u \mid s) &\propto \alpha \exp(U(u; s)) \\ P_{L_1}(s \mid u) &\propto P_{S_1}(u \mid s) P(s) \end{aligned}$$

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More at https://www.problang.org/

#### Next

Linguistic typology and computational multilingualism.